

Magnetism And Matter

NCERT Exercise Questions

3. Magnetic field strength, $B = 0.25 \text{ T}$
 Torque on the bar magnet, $T = 4.5 \times 10^{-2} \text{ J}$
 Angle between the bar magnet and the external magnetic field, 30° .

Torque is related to magnetic moment (M) as:

$$T = MB \sin \theta$$

$$\therefore M = \frac{T}{B \sin \theta}$$

$$= \frac{4.5 \times 10^{-2}}{0.25 \times \sin 30^\circ} = 0.36 \text{ JT}^{-1}$$

Hence, the magnetic moment of the magnet is 0.36 JT^{-1} .

4. Moment of the bar magnet, $M = 0.32 \text{ JT}^{-1}$
 External magnetic field, $B = 0.15 \text{ T}$

- a) When the bar magnet is aligned along the magnetic field, it is considered as being in stable equilibrium. Hence, the angle θ , between the bar magnet and the magnetic field is 0° .

$$\begin{aligned} \text{Potential energy of the system} &= -MB \cos \theta \\ &= -0.32 \times 0.15 \cos 0^\circ \\ &= -4.8 \times 10^{-2} \text{ J} \end{aligned}$$

- b) When the bar magnet is aligned opposite to the magnetic field, it is considered as being in unstable equilibrium, $\theta = 180^\circ$.
 Potential energy = $-MB \cos \theta$
- $$\begin{aligned} &= -0.32 \times 0.15 \cos 180^\circ \\ &= 4.8 \times 10^{-2} \text{ J} \end{aligned}$$

5. Number of turns in the solenoid, $n = 800$

Area of cross-section, $A = 2.5 \times 10^{-4} \text{ m}^2$

Current in the solenoid, $I = 3.0 \text{ A}$

A current-carrying solenoid behaves as a bar magnet because a magnetic field develops along its axis, i.e., along its length.

The magnetic moment associated with the given current-carrying solenoid is calculated as:

$$M = nIA$$

$$= 800 \times 3.0 \times 2.5 \times 10^{-4}$$

$$= 0.6 \text{ JT}^{-1}$$

8. Number of turns on the solenoid, $n = 2000$

Area of cross-section of the solenoid, $A = 1.6 \times 10^{-4} \text{ m}^2$

Current in the solenoid, $I = 4 \text{ A}$

a) The magnetic moment along the axis of the solenoid is calculated as:

$$M = nAI$$

$$= 2000 \times 1.6 \times 10^{-4} \times 4$$

$$= 1.28 \text{ Am}^2$$

b) Angle betⁿ the magnetic field and the axis of the solenoid $\theta = 30^\circ$

$$\text{Torque, } \tau = MB \sin \theta$$

$$= 1.28 \times 7.5 \times 10^{-2} \sin 30^\circ$$

$$= 4.8 \times 10^{-2} \text{ Nm}$$

Since the magnetic field is uniform, the force on the solenoid is zero. The torque on the solenoid is $4.8 \times 10^{-2} \text{ Nm}$.

9. $N = 16$

$r = 10 \text{ cm} = 0.1 \text{ m}$

$A = \pi r^2 = \pi \times (0.1)^2 \text{ m}^2$

$I = 0.75 \text{ A}$

$B = 5.0 \times 10^{-2} \text{ T}$

$v = 2.0 \text{ s}^{-1}$

$$\begin{aligned}
 M &= NIA = NI\pi r^2 \\
 &= 16 \times 0.75 \times \pi \times (0.1)^2 \\
 &= 0.377 \text{ JT}^{-1}
 \end{aligned}$$

Frequency is given by the relation:

$$v = \frac{1}{2\pi} \sqrt{\frac{MB}{I}}$$

where,

$I =$ moment of inertia of the coil

$$\begin{aligned}
 \therefore I &= \frac{MB}{4\pi^2 v^2} \\
 &= \frac{0.377 \times 5 \times 10^{-2}}{4\pi^2 \times (2)^2} \\
 &= 1.19 \times 10^{-1} \text{ Kg m}^2
 \end{aligned}$$

Hence, the moment of inertia of the coil about its axis of rotation is $1.19 \times 10^{-1} \text{ Kg m}^2$.

11. Angle of declination, $\theta = 12^\circ$

Angle of dip, $\delta = 60^\circ$

$B_H = 0.16 \text{ G}$

Earth's magnetic field at the given location = B

We can relate B and B_H as:

$$B_H = B \cos \delta$$

$$\therefore B = \frac{B_H}{\cos \delta}$$

$$= \frac{0.16}{\cos 60^\circ} = 0.32 \text{ G}$$

13. Earth's magnetic field at the given place, $H = 0.36 \text{ G}$
The magnetic field at a distance d , on the axis of the magnet is given as:

Where,

μ_0 = Permeability of free space

M = Magnetic moment

The magnetic field at the same distance d , on the equatorial line of the magnet is given as:

$$B_2 = \frac{\mu_0 M}{4\pi d^3} = \frac{H}{2} \quad [\text{using eq (i)}]$$

Total magnetic field, $B = B_1 + B_2$

$$H + \frac{H}{2}$$

$$= 0.36 + 0.18 = 0.54 \text{ G}$$

Hence, the magnetic field is 0.54 G in the direction of earth's magnetic field

18. Current I in the wire, $I = 2.5 \text{ A}$

Angle of dip at the given location on earth, $\delta = 0^\circ$
Earth's magnetic field, $H = 0.33 \text{ G} = 0.33 \times 10^{-4} \text{ T}$

The horizontal component of earth's magnetic field is given as ¹⁰

$$H_H = H \cos \delta$$

$$= 0.33 \times 10^{-4} \times \cos 0^\circ = 0.33 \times 10^{-4}$$

The magnetic field at the neutral point at a distance R from the cable is given by the relation

$$H_H = \frac{\mu_0 I}{2\pi R}$$

Where ,

$$\mu_0 = \text{Permeability of free space} = 4\pi \times 10^{-7} \text{ Tm A}^{-1}$$

$$\therefore R = \frac{\mu_0 I}{2\pi H_H}$$

$$= \frac{4\pi \times 10^{-7} \times 2.5}{2\pi \times 0.33 \times 10^{-4}} = 15.15 \times 10^{-3} \text{ m} = 1.51 \text{ cm}$$

Hence, a set of neutral point lie on a straight line parallel to the cable at a perpendicular distance of 1.51 cm, above the plane of the paper.