

MAGNETISM AND MATTER



S.3) Magnetic field strength, $B = 0.25 \text{ T}$
Torque on the bar magnet, $\tau = 4.5 \times 10^{-2} \text{ J}$

The angle between the bar magnet and the external magnetic field, $\theta = 30^\circ$.

Torque is related to magnetic moment (M) as:

$$\tau = MB \sin \theta$$

$$\therefore M = \frac{\tau}{B \sin \theta}$$

$$= \frac{4.5 \times 10^{-2}}{0.25 \times \sin 30^\circ} = 0.36 \text{ J T}^{-1}$$

Hence, the magnetic moment of the magnet is 0.36 J T^{-1} .

S.4) Moment of the bar magnet, $M = 0.32 \text{ J T}^{-1}$
External magnetic field, $B = 0.15 \text{ T}$

(a) The bar magnet is aligned along the magnetic field. This system is considered as being in stable equilibrium.

Hence, the angle θ , between the bar magnet and the magnetic field is 0° .

Potential energy of the system = $-MB \cos \theta$

$$= -0.32 \times 0.15 \cos 0^\circ$$

$$= -4.8 \times 10^{-2} \text{ J}$$

(b) The bar magnet is oriented 180° to the magnetic field. Hence, it is in unstable equilibrium.
 $\theta = 180^\circ$



$$\begin{aligned}\text{Potential energy} &= -M B \cos \theta \\ &= -0.82 \times 0.15 \cos 180^\circ \\ &= 4.8 \times 10^{-2} \text{ J}\end{aligned}$$

5.5) Number of turns in the solenoid, $n = 800$
Area of cross-section, $A = 2.5 \times 10^{-4} \text{ m}^2$
Current in the solenoid, $I = 3.0 \text{ A}$

$$\begin{aligned}M &= n I A \\ &= 800 \times 3 \times 2.5 \times 10^{-4} \\ &= 0.6 \text{ J T}^{-1}\end{aligned}$$

5.8) $n = 2000$
 $A = 1.6 \times 10^{-4} \text{ m}^2$
 $I = 4.0 \text{ A}$

$$\begin{aligned}\text{(a)} \quad M &= n A I \\ &= 2000 \times 4 \times 1.6 \times 10^{-4} \\ &= 1.28 \text{ A m}^2\end{aligned}$$

(b) $B = 7.5 \times 10^{-2} \text{ T}$
 $\theta = 30^\circ$

$$\begin{aligned}\tau &= M B \sin \theta \\ &= 1.28 \times 7.5 \times 10^{-2} \sin 30^\circ \\ &= 0.048 \text{ J}\end{aligned}$$

Since the magnetic field is uniform, the force on the solenoid is zero. The torque on the solenoid is 0.048 J

5.9) $N = 16$
 $r = 10 \text{ cm} = 0.1 \text{ m}$
 $A = \pi r^2 = \pi \times (0.1)^2 \text{ m}^2$
 $I = 0.75 \text{ A}$
 $B = 5.0 \times 10^{-2} \text{ T}$

$$v = 201 \text{ m}^{-1}$$

$$M = NIA = N I \pi r^2$$

$$16 \times 0.15 \times \pi \times (0.1)^2$$

$$= 0.377 \text{ J T}^{-1}$$

$$v = \frac{1}{2\pi} \sqrt{\frac{MB}{I}}$$

$$\therefore I = \frac{MB}{4\pi^2 v^2}$$

$$= \frac{0.377 \times 5 \times 10^{-2}}{4\pi^2 \times (2)^2}$$

$$= 1.2 \times 10^{-4} \text{ kg m}^2$$

5.11) $\theta = 12^\circ$
 $\delta = 60^\circ$
 $B_H = 0.16 \text{ G}$

$$B_H = B \cos \delta$$

$$\therefore B = \frac{B_H}{\cos \delta}$$

$$= \frac{0.16}{\cos 60} = 0.32 \text{ G}$$

5.13) $M = 0.36 \text{ G}$
 $B_1 = \frac{\mu_0 M}{4\pi d^3} = H \quad \text{--- (1)}$

$$B_2 = \frac{\mu_0 M}{4\pi d^3} = \frac{H}{2}$$

$$B = B_1 + B_2$$

$$= H + \frac{H}{2}$$

$$= 0.36 + 0.18 = 0.54 \text{ G}$$

5.18) Current in the wire = 2.5 A

$$R = 0.33 \text{ } \Omega = 0.33 \times 10^{-4} \text{ } \Omega$$

$$B = 0$$

$$B_H = R \cos \delta = 0.33 \times 10^{-4} \cos 0 = 0.33 \times 10^{-4} \text{ } \Omega$$

$$B_C = (\mu_0 / 2\pi) \times (I/r)$$

$$B_C = (4\pi \times 10^{-7} / 2\pi) \times (2.5/r) = (5 \times 10^{-7} / r)$$

$$B_H = B_C$$

$$0.33 \times 10^{-4} = 5 \times 10^{-7} / r$$

$$r = 5 \times 10^{-7} / 0.33 \times 10^{-4}$$

$$= 0.015 \text{ m} = 1.5 \text{ cm}$$