

H.C.F AND L.C.M

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 08

CHAPTER NAME :H.C.F and L.C.M

SUBTOPIC : RECAPITULATION OF THE CHAPTER

PERIOD NO: 4

CHANGING YOUR TOMORROW

Learning outcomes

- Students will be able to find prime factors of a given number.
- Students will be able to find H.C.F of given pair of numbers .
- Students will develop application skill.
- Students will be able to find L.C.M. of given numbers .
- Students will be able to solve problems based on LCM .

PREVIOUS KNOWLEDGE TEST

Question 1.

State true or false : Give an example.

- (i) H.C.F. of two prime numbers is 1.
- (ii) H.C.F. of two co-prime numbers is 1.
- (iii) L.C.M. of two prime numbers is equal to their product.
- (iv) L.C.M. of two co-prime numbers is equal to their product.

PREVIOUS KNOWLEDGE TEST

Solution:

- (i) True : Because the prime numbers have no common factor except 1.
- (ii) True : Because co-prime numbers have no common factor except 1.
- (iii) True : Because the prime number have no common factor except 1.
- (iv) True : Because co-prime numbers have no common factor except 1.

EVALUATION QUESTION (EX-8C)

Question 1.

Find the H.C.F. of :

- (i) 108, 288 and 420
- (ii) 36, 54 and 138

Solution:

(i) H.C.F. of 108, 288, 420 = 12

$$\begin{array}{r} 108 \overline{)288(2} \\ 216 \\ \hline 72 \overline{)108(1} \\ 72 \\ \hline 36 \overline{)72(2} \\ 72 \\ \hline \times \end{array}$$

$$\begin{array}{r} 36 \overline{)420(11} \\ 396 \\ \hline 24 \overline{)36(1} \\ 24 \\ \hline 12 \overline{)24(2} \\ 24 \\ \hline \times \end{array}$$

(ii) H.C.F. of 36, 54 and 138 = 6

$$\begin{array}{r} 36 \overline{)54(1} \\ 36 \\ \hline 18 \overline{)36(2} \\ 36 \\ \hline \times \end{array} \quad \begin{array}{r} 18 \overline{)138(7} \\ 126 \\ \hline 12 \overline{)18(1} \\ 12 \\ \hline 6 \overline{)12(2} \\ 12 \\ \hline \times \end{array}$$

Evaluation Question

Question 2.

Find the L.C.M. of:

(i) 72, 80 and 252

(ii) 48, 66 and 120

Solution:

L.C.M. 72, 80, 252

$$= 2 \times 2 \times 2 \times 3 \times 3 \times 10 \times 7 = 5040$$

(ii) L.C.M. of 48, 66 and 120

2	72, 80, 252
2	36, 40, 126
2	18, 20, 63
3	9, 10, 63
3	3, 10, 21
	1, 10, 7

2	48, 66, 120
2	24, 33, 60
2	12, 33, 30
3	6, 33, 15
	2, 11, 5

$$= 2 \times 2 \times 2 \times 2 \times 3 \times 5 \times 11 = 2640$$

Evaluation Question

Question 4.

The product of two numbers is 12096 and their H.C.F. is 36. Find their L.C.M.

Solution:

We know that

Product of two numbers = Product of their H.C.F. and L.C.M.

$$\Rightarrow 12096 = 36 \times \text{L.C.M.}$$

$$\Rightarrow \text{L.C.M.} = 12096/36 = 336$$

Evaluation Question

Question 5.

The product of the H.C.F. and the L.C.M. of two numbers is 1152. If one number is 48, find the other one.

Solution:

We know that:

Product of two numbers = Product of their H.C.F. and L.C.M.

\Rightarrow 1st number \times 2nd number = Product of their H.C.F. and L.C.M.

$\Rightarrow 48 \times \text{2nd number} = 1152$

$\Rightarrow \text{2nd number} = 1152/48 = 24$

Evaluation Question

Question 6.

- (i) Find the smallest number that is completely divisible by 28 and 42.
- (ii) Find the largest number that can divide 28 and 42 completely.

Solution:

- (i) We know that the least number which is divisible by 28 and 42 is their L.C.M.

$$\text{L.C.M. of 28 and 42} = 2 \times 2 \times 3 \times 7 = 84$$

- (ii) We know that the largest number which can divide 28 and 42 completely will be their H.C.F.

$$\text{H.C.F. of 28 and 42} = 14$$

$$\begin{array}{r} 2 \mid 28, 42 \\ 7 \mid 14, 21 \\ \hline & 2, 3 \end{array}$$

$$\begin{array}{r} 28 \overline{)42(} 1 \\ 28 \\ \hline 14 \end{array} \begin{array}{r} 28 \overline{)28(} 2 \\ 28 \\ \hline \times \end{array}$$

Evaluation Question

Question 7.

Find the L.C.M. of 140 and 168. Use the L.C.M. obtained to find the H.C.F. of the given numbers.

Solution:

Numbers are 140 and 168

L.C.M. of 140 and 168

2	140, 168
2	70, 84
7	35, 42
	5, 6

$$= 2 \times 2 \times 7 \times 5 \times 6 = 840$$

$$\text{H.C.F.} = \frac{\text{1st number} \times \text{2nd number}}{\text{L.C.M.}}$$

$$= \frac{140 \times 168}{840} = 28$$

Evaluation Question

Question 8.

Find the H.C.F. of 108 and 450 and use the H.C.F. obtained to find the L.C.M. of the given numbers.

Solution:

Numbers are given : 108 and 450

H.C.F. of 108 and 450= 18

$$\begin{array}{r} 108 \overline{)450(4} \\ 432 \\ \hline 18 \end{array} \begin{array}{r} 108(6 \\ \hline \times \end{array}$$

$$\therefore \text{L.C.M.} = \frac{1\text{st number} \times 2\text{nd number}}{\text{H.C.F.}}$$

$$= \frac{108 \times 450}{18} = 2700$$

Homework

HW
Ex.8C

AHA

1. The traffic lights at three different road crossing change after every 48 sec, 72 sec and 108 sec respectively. If they change simultaneously at 7:00 am, at what time will they change simultaneously again?
2. Three tankers contain 403 litres, 434 litres and 465 litres of diesel. Find maximum capacity of a container that can measure the diesel of the three containers exact number of times.

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