



# **POLYNOMIALS**

## INTRODUCTION

**SUBJECT : MATHEMATICS**  
**CHAPTER NUMBER: 02**  
**CHAPTER NAME : POLYNOMIALS**

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**CHANGING YOUR TOMORROW**

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## Learning outcome

- 1..Students will be able to define polynomial.
- 2.Students will be able to know the types of polynomials.
- 3.Students will be able to know the general form of linear, quadratic & cubic polynomial.
4. .Students will be able to know geometrical meaning of the zeros of a polynomial.

Introduction about polynomials ,its types and zero of a polynomial.

<https://youtu.be/NmpmGuNNqfI> {4.50}



## POLYNOMIALS IN ONE VARIABLE

- **A *polynomial p(x) in one variable x*** is an algebraic expression in x of the form

$p(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$  where  $a_0, a_1, a_2, \dots, a_n$  are constants (real numbers) and  $a_n \neq 0$ .

$a_0, a_1, a_2, \dots, a_n$  are respectively the **coefficients** and **n** is called **the degree of the polynomial**. Each of  $a_n x^n, a_{n-1} x^{n-1}, \dots, a_0$  is called a **term** of the polynomial  $p(x)$ .

- ↳ Geometrical meaning of the zeroes of a polynomial
- ↳ <https://youtu.be/mBF7Gd7eiNo> {5.32}

A real number 'a' is a **zero of a polynomial**  $p(x)$  if

$p(a) = 0$ . In this case,  $a$  is also called a *root* of the equation  $p(x) = 0$ .

Every **linear polynomial** in one variable has a **unique zero**, a non-zero constant polynomial has no zero, and every real number is a zero of the zero polynomial.

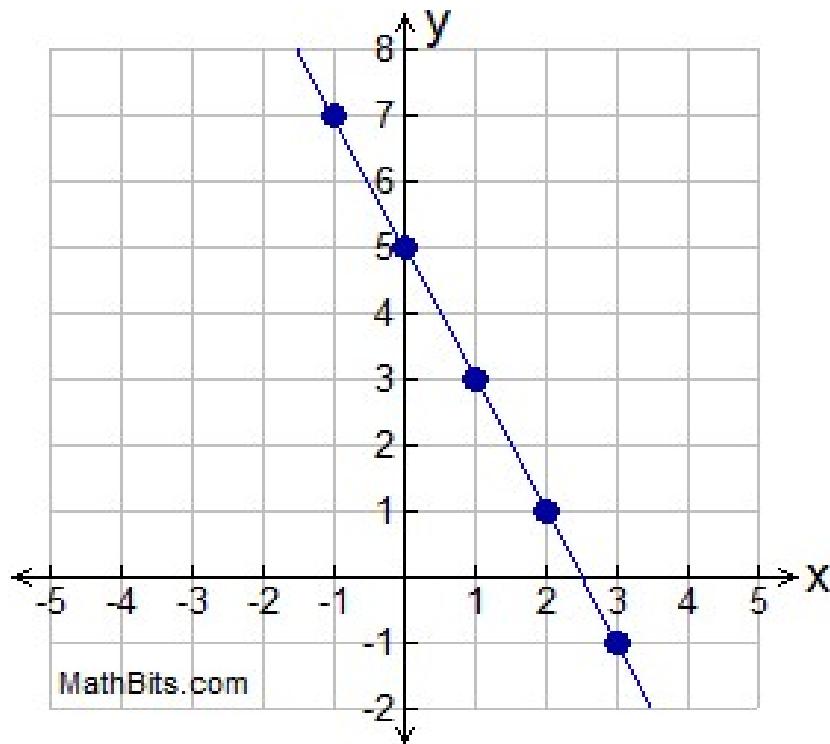
A **quadratic polynomial** can have at most **2 zeroes** and a **cubic polynomial** can have atmost **3 zeroes**

### Geometrical Meaning of the Zeroes of a Polynomial

The linear polynomial  $ax + b$ ,  $a \neq 0$ , has exactly one zero, namely  $-b/a$  the  $x$ -coordinate of the point where the graph of  $y = ax + b$  intersects the  $x$ -axis. Example : The zero of the linear polynomial

$-2x + 5$  is  $5/2$  the point where the graph linear equation  $y = -2x + 5$  meets the  $x$  axis.

## GRAPH OF LINEAR EQUATION $Y= -2x + 5$



For any quadratic polynomial  $ax^2 + bx + c$ ,  $a \neq 0$ , the graph of the corresponding equation

$y = ax^2 + bx + c$  has one of the two shapes U either open upwards or open downwards depending on whether  $a > 0$  or  $a < 0$ .

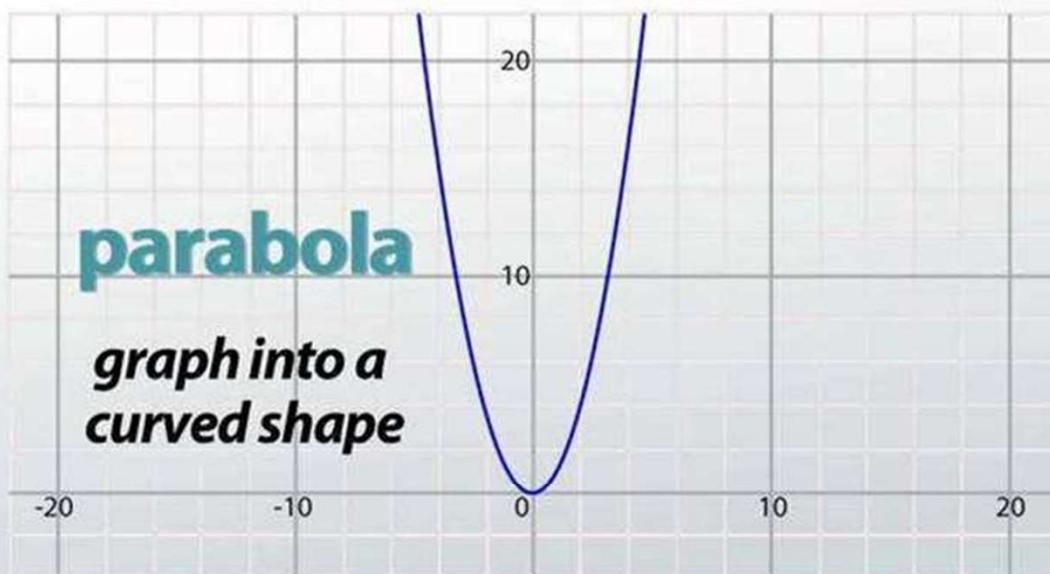
These curves are called **parabolas**.

**A parabola is a plane curve which is mirrorsymmetrical and approximately U-shaped.**

## GRAPHING QUADRATIC FUNCTIONS

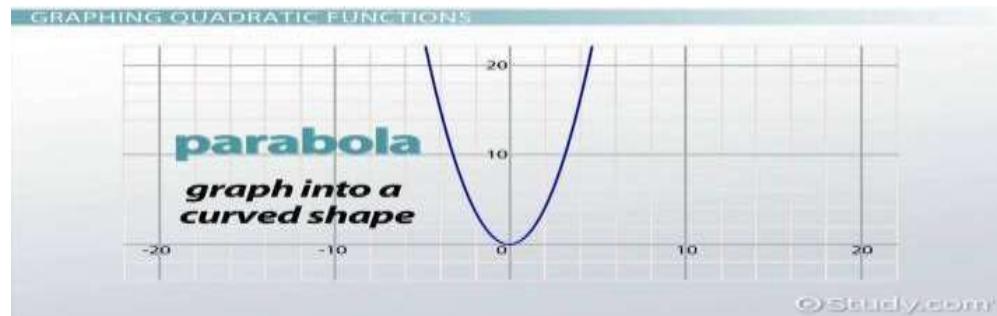
**parabola**

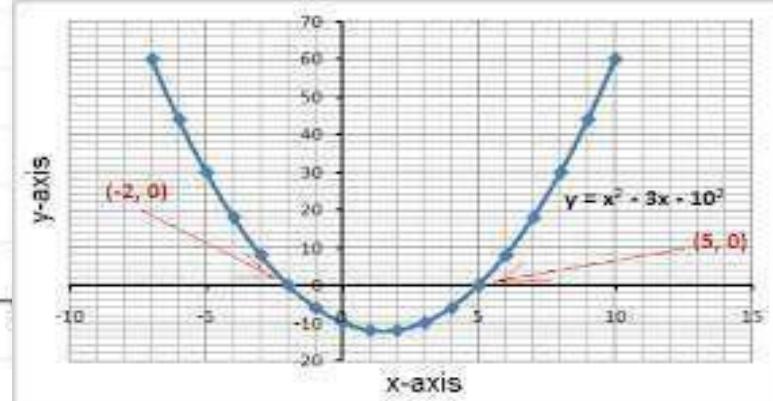
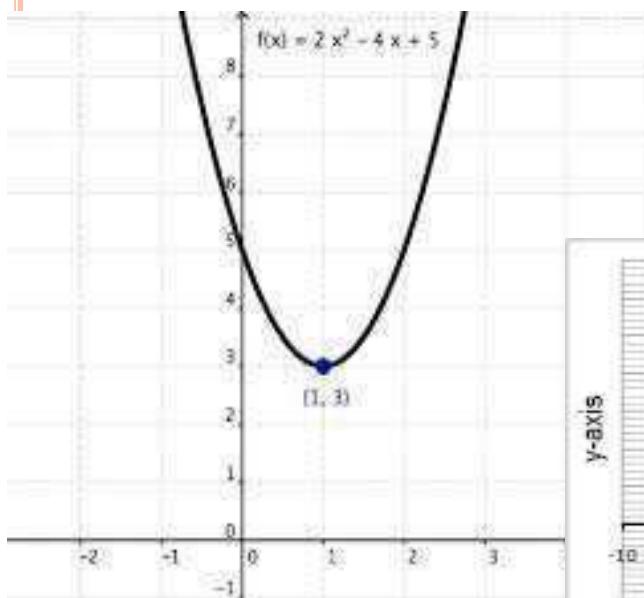
*graph into a  
curved shape*



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- The zeroes of a quadratic polynomial  $ax^2 + bx + c$ ,  $a \neq 0$ , are precisely the **x**-coordinates of the points where the **parabola** representing  $y = ax^2 + bx + c$  intersects the **x-axis**
- We can see geometrically, from the following graphs, that a quadratic polynomial can have either two distinct zeroes or two equal zeroes (i.e., one zero), or no zero. This also means that a polynomial of degree 2 has at most two zeroes





General form of linear polynomials  $ax + b$  where  $a \neq 0$

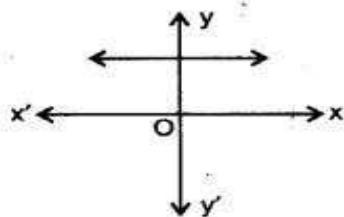
General form of quadratic polynomials  $ax^2 + bx + c$  where  $a \neq 0$

General form of cubic polynomial  $ax^3 + bx^2 + cx + d$ , where  $a \neq 0$ ,



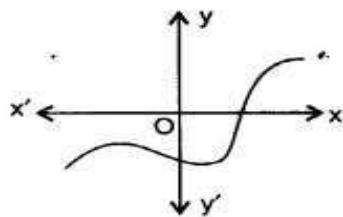
The number of zeroes of  $p(x)$  in each graph given; are

(i)



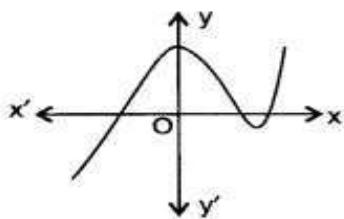
This graph shows  $p(x)$  has no zero.

(ii)



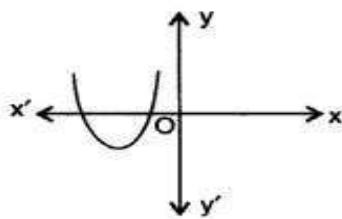
This graph shows  $p(x)$  has one zero.

(iii)



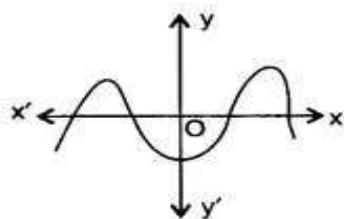
This graph shows  $p(x)$  has three zeroes.

(iv)



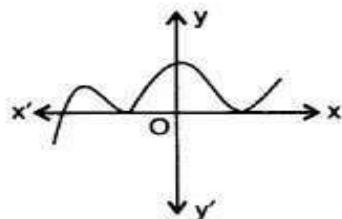
This graph shows  $p(x)$  has two zeroes.

(v)



This graph shows  $p(x)$  has four zeroes.

(vi)



This graph shows  $p(x)$  has three zeroes.

## HOME ASSIGNMENT Ex. 2.1 Q. No 1

AHA

1. Draw the graph of  $x^2-3x-4$
2. Draw the graph of  $x^3-4x$

**THANKING YOU  
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